Marginal Nature of DNA solutions

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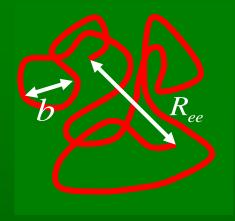
Polymer physics starts with simple intuitive models

Take into account non-idealities => drastic change in the behavior of the models => require mathematically complicated models

The intuitive models remain ideal models without real-life examples

DNA to the rescue !

Ideal Polymer – random walk in space



Measure of flexibility: *b* - Kuhn length

$$N = \frac{L}{b} \qquad \langle R_{ee}^2 \rangle = Nb^2 = Lb$$

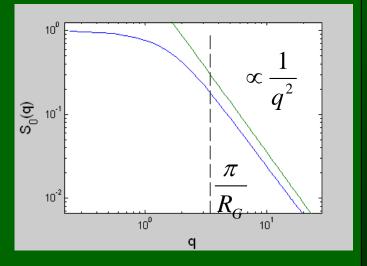
$$R_g \propto b\sqrt{N}$$

$$P(\vec{R}_{ee}) \propto \exp\left(-\frac{3R_{ee}^2}{2\langle R_{ee}^2 \rangle}\right)$$

Solution structure:

$$S_{0}(\vec{q}) = \frac{2}{(qR_{G})^{4}} \left[q^{2}R_{G}^{2} - 1 + \exp\left(-q^{2}R_{G}^{2}\right) \right]$$

Debye function



Real Polymer – self-avoiding random walk in space

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excluded volume interactions (Flory)

$$\left\langle R_{ee}^2 \right\rangle \propto N^{3/5}$$

$$r < R_G$$

 $\overline{R_{c}}$

$$g(r) \propto \frac{n}{r^3} \propto \frac{r^{5/3}}{r^3} \propto \frac{r}{r}$$

DNA is semiflexible polymer – nearly ideal for contour lengths:

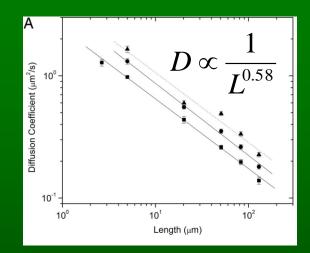
$$L \sim \left(\frac{b}{d}\right)^2 b \sim 60 \,\mu m$$

b – DNA Kuhn length (100 nm)d – double helix diameter (2 nm)

Experiments:

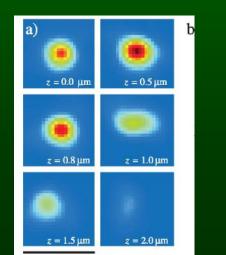
 70-90s: static light scattering show ~30% coil (radius) expansion for 14µm DNA

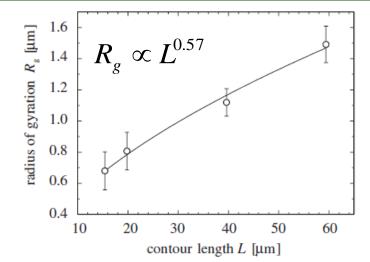
-Diffusion of single DNA molecules vs. length Robertson, Laib, Smith PNAS 2006



-segment distribution of end-tethered DNA

Gisler et al, PRL 2006

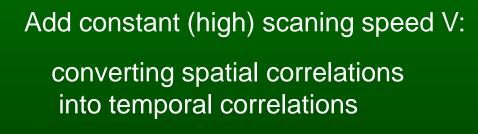


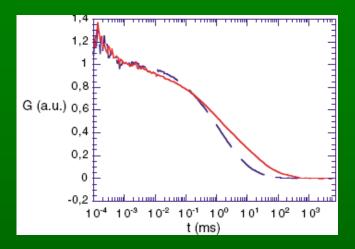


Experimental approach:Fluorescence Correlation Spectroscopy

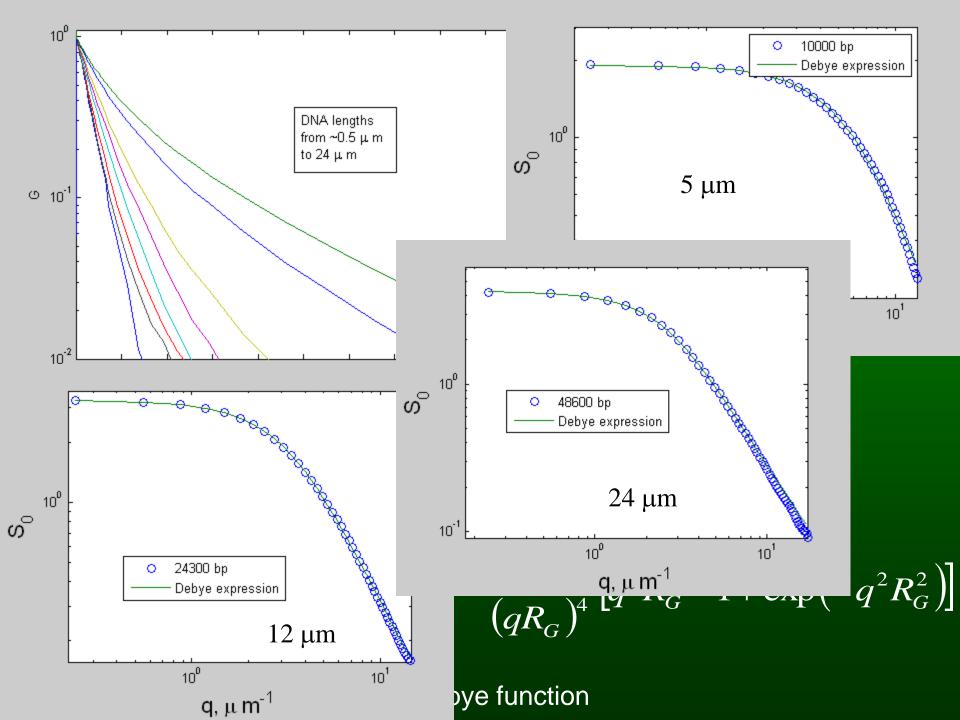


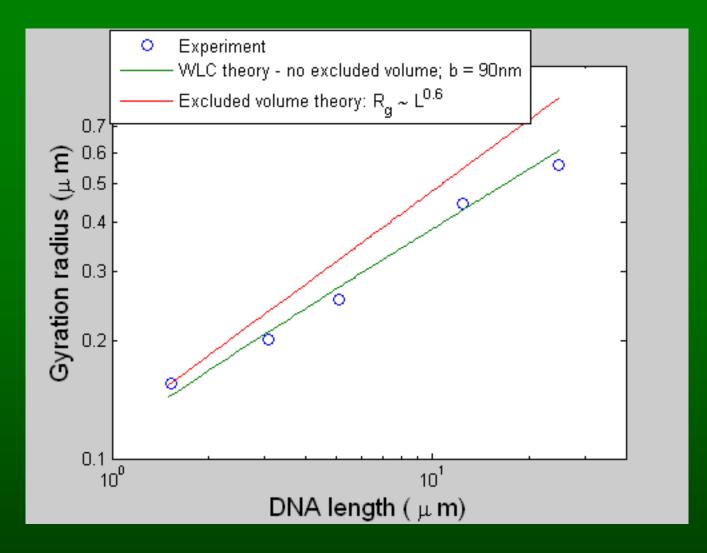
$$G(t) = \frac{1}{\overline{I}^2} \frac{1}{T} \int_0^T \delta I(t') \delta I(t'+t) dt'$$



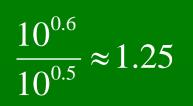


$$G(t) = \int_{0}^{t} F(\vec{r})g(\vec{r} - \vec{V}t)dt$$
$$\vec{R} = \vec{V}t$$
$$G(\vec{R}) = \int F(\vec{r})g(\vec{r} - \vec{R})dt$$
$$g(\vec{q}) \equiv S(\vec{q}) = \frac{G(\vec{q})}{(r)}$$





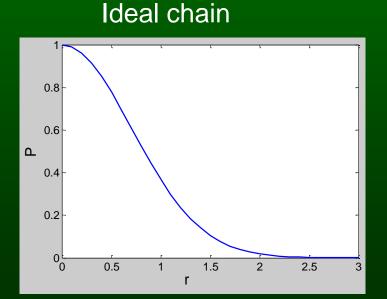
No excluded volume interactions: ideal chain !!!



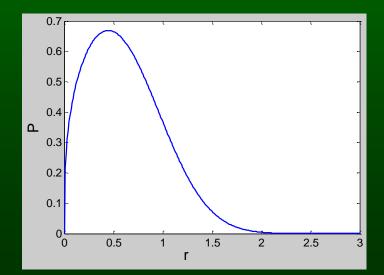
Significant when you have several decades in polymer lengths

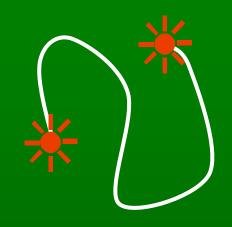
Main support for DNA ideality: Structure factor behaves as Debye function

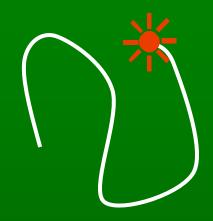
End to end distance distribution: qualitative difference in behavior

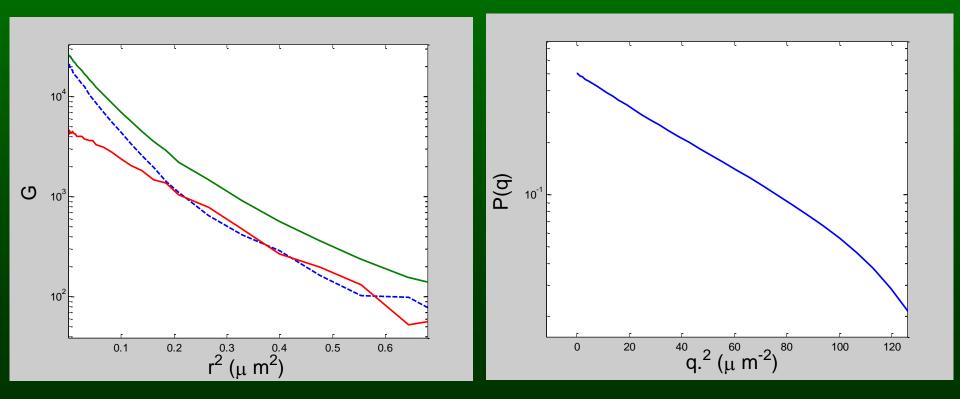


Real chain







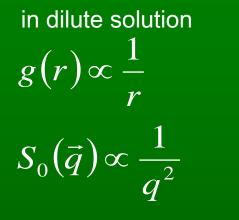


Sebiludieutegregiendes DISIANA $c \times c^*$ (overlap concentration)





Screening (Edwards, 1975): similar to Debye-Hückel theory of electrostatic screening



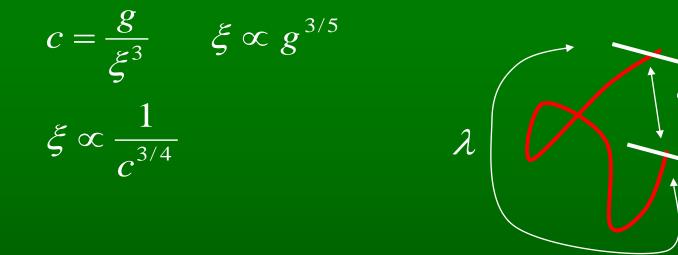
in semi-dilute solution (perturbation theory)

$$g(r) \propto \frac{1}{r} \exp\left(-\frac{r}{\xi}\right)$$

$$S(\vec{q}) \propto \frac{1}{1 + (q\xi)^2} = \frac{1}{1 + \xi^2 / S_0(q)}$$

Dependence of screening length on concentration $\lambda = gb \quad \xi^2 = gb^2$ $g = \frac{1}{cv}$ $\lambda \approx \frac{b}{cv} = \frac{\xi^2}{b}$ $\lambda \begin{pmatrix} & & & \\ & & & \\ & & \\ & & & \\ &$

Screening – scaling theory (deGennes, Pincus)

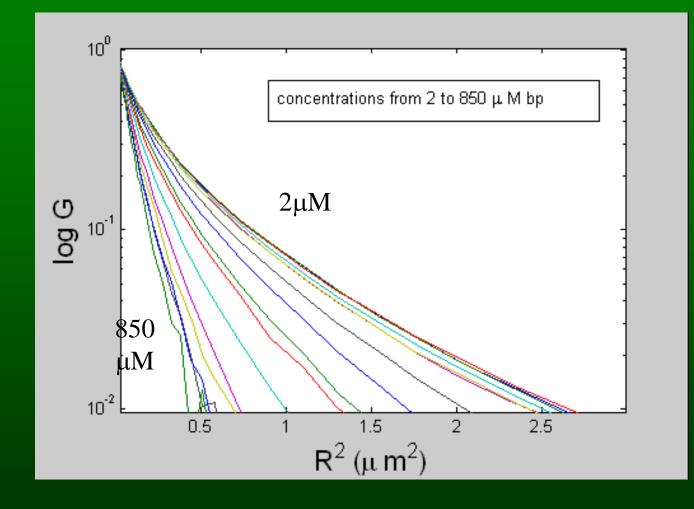


What to expect for DNA?

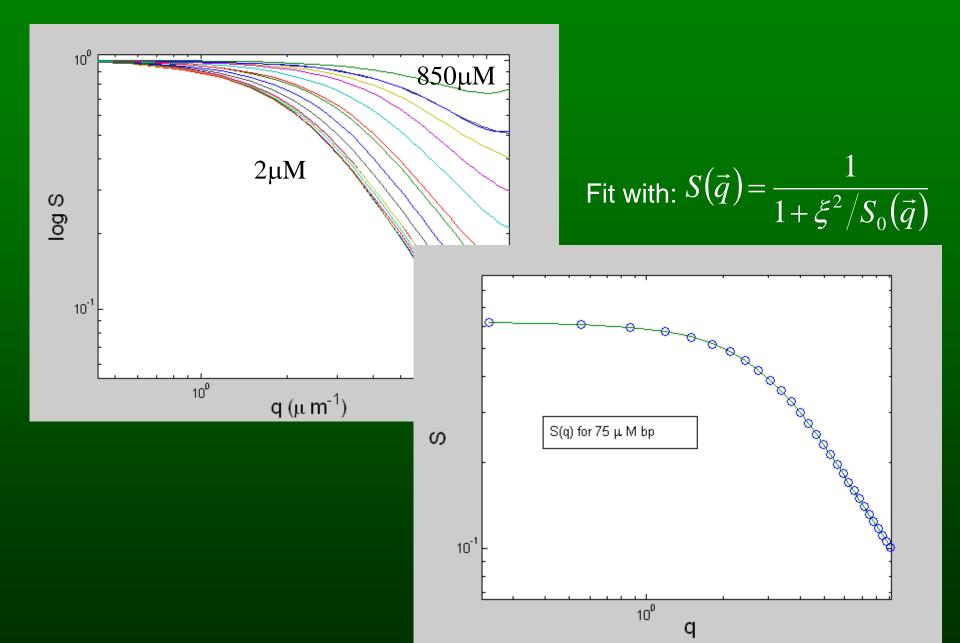
$$c = \frac{g}{\xi^3} \qquad \xi \propto g^{1/2}$$
$$\xi \propto \frac{1}{c} \qquad -?$$

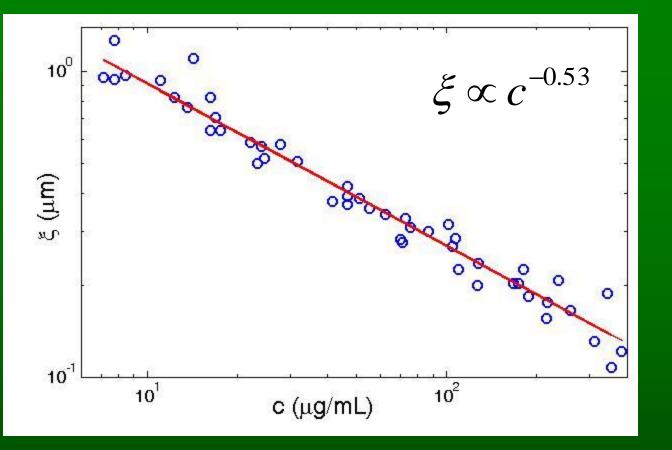
FCS correlation function vs DNA concentration

(Eyal Shafran, Alon Yaniv & O.K, PRL 104128, 2010)

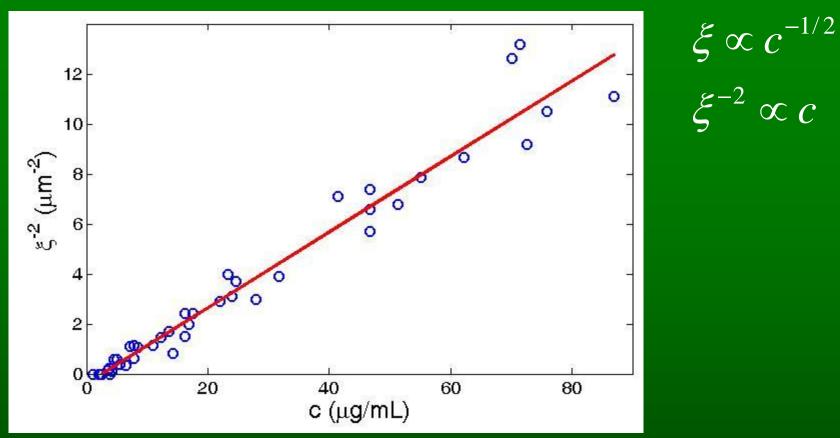


Static stucture function vs DNA concentration





Not $\sim c^{-3/4}$ and not $\sim c^{-1}$, close to $\sim c^{-1/2}$ predicted by Edwards



~ according to mean-field of Edwards

$$\xi^2 \sim \frac{b^2}{cv} \qquad \frac{d\xi^{-2}}{dc} = \frac{v}{b^2} \approx \frac{b^2 d}{b^2} = d$$

$$d \approx 3.5 nm$$

Joanny, Schaeffer, Pincus (1980):

In polymer physics we usually distinguish three types of solvents with respect to the interactions between monomers (second virial coefficient *v*):



strong excluded volume interactions – good solvents: $\xi \sim C^{-3/4}$

weak exluded volume interactions– marginal solutions: $\xi \sim C^{-1/2}$

no interactions (v = 0) – θ solvents: $\xi \sim C^{-1}$

Attractive interaction (v < 0) – bad solvents: irrelevant here

DNA:

-Nearly ideal polymer in dilute solutions -Nearly mean-field polymer in semidilute solutions

All due to stiffness

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And thank you for your attention!