

The Flavor of Higgs

*39th Johns Hopkins Workshop
Theory challenges in the LHC era*

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Plan of Talk

1. Flavor at the LHC
2. The SM flavor of h
3. The BSM flavor of h
4. $h \rightarrow \tau\mu$: Experiment
5. What if $\text{BR}(h \rightarrow \tau\mu) \sim 0.01$?
6. Conclusions

Flavor at the LHC

Questions for the LHC

- What is the mechanism of electroweak symmetry breaking?
- What separates the electroweak scale from the Planck scale?
- What happened at the electroweak phase transition?
- How was the baryon asymmetry generated?
- What are the dark matter particles?
- What is the solution of the flavor puzzles?

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The topic of this talk

The flavor puzzles

- The SM flavor puzzle:
Why is there structure in the charged fermion flavor parameters?
Smallness and hierarchy
- The SM flavor puzzle extended:
Why is the neutrino flavor structure different?
Neither smallness nor hierarchy
- The NP flavor puzzle:
If there is TeV-scale NP, why doesn't it affect FCNC?
Degeneracy and alignment

Can we make progress?

- NP that couples to quarks/leptons \implies New flavor parameters (spectrum, flavor decomposition) that can be measured
- The NP flavor structure could be:
 - MFV
 - Related but not identical to SM
 - Unrelated to SM or even anarchical
- The NP flavor puzzle:
With ATLAS/CMS we are likely to understand how it is solved
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Progress possible if structure not MFV but related to SM

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Progress possible if structure not MFV but related to SM
- h \implies The “NP” is already here!
 $Y_{\bar{f}_i f_j}$ are new flavor parameters that can be measured

The SM flavor of h

Y^F vs. M_F : SM

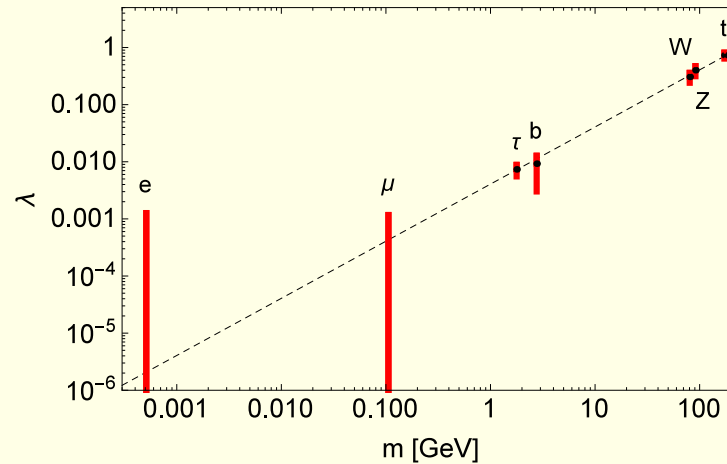
- $Y^F = \sqrt{2}M_F/v$
 - Proportionality: $y_i \equiv Y_{ii}^F \propto m_i$
 - Factor of proportionality: $y_i/m_i = \sqrt{2}/v$
 - Diagonality: $Y_{ij}^F = 0$ for $i \neq j$

Relevant data

Observable	Experiment
$R_{\gamma\gamma}$	1.14 ± 0.18
R_{ZZ^*}	1.17 ± 0.23
R_{WW^*}	0.99 ± 0.15
$R_{b\bar{b}}$	0.7 ± 0.3
$R_{\tau\tau}$	1.09 ± 0.23
$R_{\mu\mu}$	< 7
R_{ee}	$< 4 \times 10^5$

- $$R_f = \frac{\sigma_{\text{prod}} \text{BR}(h \rightarrow f)}{[\sigma_{\text{prod}} \text{BR}(h \rightarrow f)]^{\text{SM}}}$$

Proportionality?



A. Efrati

- Indication that Y_t, Y_b, Y_τ not far from SM
- $y_3/m_3 \approx \sqrt{2}/v$
- $y_e, y_\mu < y_\tau$
- The beginning of Higgs flavor physics

Diagonality?

- $\text{BR}(t \rightarrow ch) \leq 0.006$
 $\implies \sqrt{Y_{tc}^2 + Y_{ct}^2} \leq 0.14$

ATLAS, 1403.6293; CMS, 1410.2751

- $\text{BR}(h \rightarrow \tau\mu) \leq 0.015$
 $\implies \sqrt{Y_{\tau\mu}^2 + Y_{\mu\tau}^2} \leq 0.004$

CMS, 1502.07400; ATLAS, HIGG-2014-08

The BSM flavor of h

Dery, Efrati, Hochberg, YN, JHEP1305,039 [arXiv:1302.3229]

Dery, Efrati, Hiller, Hochberg, YN, JHEP1308,006 [arXiv:1304.6727]

Dery, Efrati, YN, Soreq, Susič, PRD90, 115022 [arXiv:1408.1371]

Y^F vs. M_F : BSM

- Proportionality and diagonality may be violated at tree level

- Two (or more) Higgs Doublets

Without loss of generality, $\{\phi_M, \phi_A\}$ where

$$\langle \phi_M^0 \rangle = v/\sqrt{2}, \quad \langle \phi_A^0 \rangle = 0$$

$$h = s_{\alpha-\beta} \text{Re}(\phi_M^0) + c_{\alpha-\beta} \text{Re}(\phi_A^0)$$

$$\implies Y_h^E = s_{\alpha-\beta} (\sqrt{2} M_E / v) + c_{\alpha-\beta} Y_A^E$$

- Single Higgs doublet and non-renormalizable terms

$$\frac{1}{\Lambda^2} (\phi^\dagger \phi) \phi \bar{L}_L Z^e E_R:$$

$$M_E = \frac{v}{\sqrt{2}} \left(Y^e + \frac{v^2}{2\Lambda^2} Z^e \right), \quad Y^E = Y^e + 3 \frac{v^2}{2\Lambda^2} Z^e$$

$$\implies Y^E = (\sqrt{2} M_E / v) + \frac{v^2}{2\Lambda^2} Z^e$$

Leptonic observables

Observable ($\ell = e, \mu$)	SM	Test
$R_{\tau^+\tau^-}$	1	Factor
$X_{\ell\ell} = \frac{\text{BR}(h \rightarrow \ell^+\ell^-)}{\text{BR}(h \rightarrow \tau^+\tau^-)}$	$(m_\ell/m_\tau)^2$	Proportionality
$X_{\ell\tau} = \frac{\text{BR}(h \rightarrow \ell^\pm\tau^\mp)}{\text{BR}(h \rightarrow \tau^+\tau^-)}$	0	Diagonality

- What can we learn from $R_{\tau\tau}$, $X_{\ell\ell}$, $X_{\ell\tau}$?

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- What can we learn from $R_{\tau\tau}$, $X_{\ell\ell}$, $X_{\ell\tau}$?
- ATLAS/CMS:
 - $R_{\tau\tau} = 1.09 \pm 0.23$
 - $X_{\mu\mu} < 12(m_\mu/m_\tau)^2 \sim 0.05$, $X_{ee} < 7 \times 10^5 (m_e/m_\tau)^2 \sim 0.06$
 - $X_{\mu\tau} = 0.14 \pm 0.06 < 0.3$

Natural Flavor Conservation (NFC)

- A solution to the 2HDM flavor puzzle
- NFC \equiv Each fermion sector (U, D, E) couples to a single Higgs doublet
- Type II: $\bar{Q}Y^U U\phi_2 + \bar{Q}Y^D D\phi_1 + \bar{L}Y^E E\phi_1$
- $Y_h^E = (\sin \alpha / \cos \beta)(\sqrt{2}M_E/v)$
- Proportionality and diagonality maintained, but with a different factor of proportionality

Minimal Flavor Violation (MFV)

- A solution to the NP flavor puzzle
- SM: When $Y^F = 0 \implies$ A large global symmetry
 $SU(3)_Q \times SU(3)_U \times SU(3)_D \times SU(3)_L \times SU(3)_E$
- MFV \equiv The only NP breaking of the $SU(3)^5$ symmetry:
 $Y^U(3, \bar{3}, 0, 0, 0)$, $Y^D(3, 0, \bar{3}, 0, 0)$, $Y^E(0, 0, 0, 3, \bar{3})$
- Example: $\frac{1}{\Lambda^2} (\phi^\dagger \phi) \overline{L_{Li}} Z_{ij}^e \phi E_{Rj}$
- $Z^e = (a + bY^{E\dagger}Y^E)Y^E$
- Proportionality violated, diagonality maintained

The Froggatt-Nielsen mechanism (FN)

- A solution to both the SM and the NP flavor puzzles
- A $U(1)_H$ symmetry broken by a small spurion $\epsilon_H(-1) \ll 1$
- Example: $\frac{1}{\Lambda^2} (\phi^\dagger \phi) \overline{L}_{Li} Z_{ij}^e \phi E_{Rj}$
- $Z_{ij}^e = \mathcal{O}(y_j |U_{ij}|)$
- Proportionality and diagonality violated

Flavor models

- 2HDM with Type II NFC
 - Universal correction to the diagonal couplings
- SM-EFT with MFV
 - Non-universal correction to the diagonal couplings
- SM-EFT with FN
 - Non-universal correction to the diagonal couplings + Off-diagonal couplings

Higgs Physics = new flavor arena

Model	$Y_\tau^2 / (2m_\tau^2 / v^2)$	$(Y_\mu^2 / Y_\tau^2) / (m_\mu^2 / m_\tau^2)$	$Y_{\mu\tau}^2 / Y_\tau^2$
SM	1	1	0
NFC-II	$(\sin \alpha / \cos \beta)^2$	1	0
MFV	$1 + 2av^2 / \Lambda^2$	$1 - 4bm_\tau^2 / \Lambda^2$	0
FN	$1 + \mathcal{O}(v^2 / \Lambda^2)$	$1 + \mathcal{O}(v^2 / \Lambda^2)$	$\mathcal{O}(U_{23} ^2 v^4 / \Lambda^4)$
GL	9	25/9	$\mathcal{O}(10^{-2})$

Dery, Efrati, Hochberg, YN, JHEP1305,039 [arXiv:1302.3229]

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Measuring Y_{ij} can probe flavor models

$h \rightarrow \tau\mu$: Experiment

Shikma Bressler, Avital Dery, Aielet Efrati, PRD 90 (2014) 015025 [1405.3229]

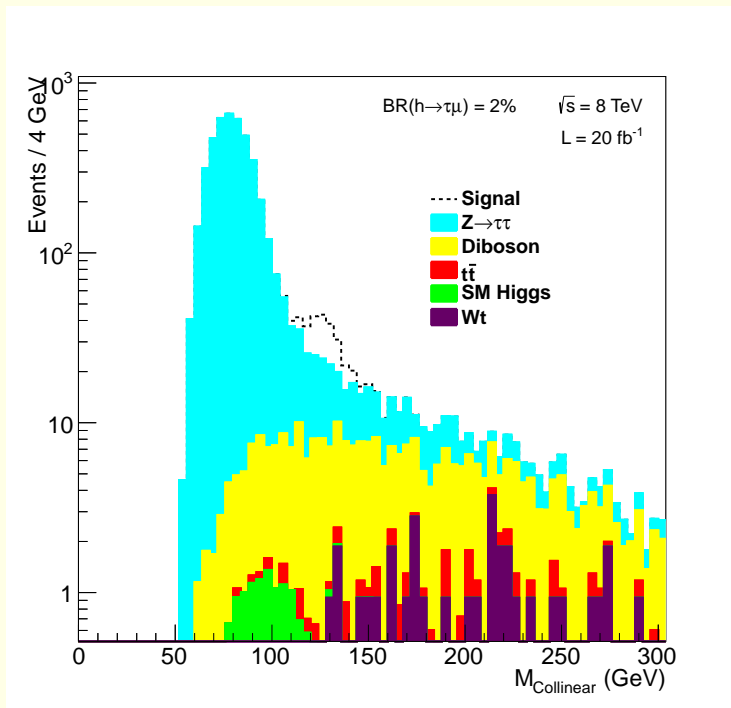
Experimental results

- CMS $h \rightarrow \mu\tau_e, h \rightarrow \mu\tau_h$ [1502.07400]:
 - $\text{BR}(h \rightarrow \tau\mu) < 1.51 \times 10^{-2}$
 - $\text{BR}(h \rightarrow \tau\mu) = (0.84_{-0.37}^{+0.39}) \times 10^{-2}$
- ATLAS $h \rightarrow \mu\tau_h$ [HIGG-2014-08]:
 - $\text{BR}(h \rightarrow \tau\mu) < 1.85 \times 10^{-2}$
 - $\text{BR}(h \rightarrow \tau\mu) = (0.77 \pm 0.62) \times 10^{-2}$
- ATLAS $e \leftrightarrow \mu$ asymmetry:
 - $\text{BR}(h \rightarrow \tau\mu) < \dots$ – Soon to appear

The problem

- Consider the following signal processes:
 - $h \rightarrow \tau^\pm \mu^\mp$ followed by $\tau^\pm \rightarrow e^\pm \nu \bar{\nu}$
 - $h \rightarrow \tau^\pm e^\mp$ followed by $\tau^\pm \rightarrow \mu^\pm \nu \bar{\nu}$
- The signal: $\mu^\pm e^\mp \cancel{E}_T$
- SM background:
 - (i) $Z \rightarrow \tau^+ \tau^- \rightarrow \mu^\pm e^\mp \cancel{E}_T$
 - (ii) $W^+ W^- \rightarrow \mu^\pm e^\mp \cancel{E}_T$
- Problem: signal lies in transitional region between (i) and (ii)
- Extrapolations from outside Higgs window inadequate;
Monte-Carlo uncertain

Background and signal



Simulated background+signal

The theoretical input

- The SM gauge interactions are lepton flavor universal
- m_e, m_μ are negligible in the relevant processes
- \implies SM processes symmetric under $e \leftrightarrow \mu$

The theoretical input

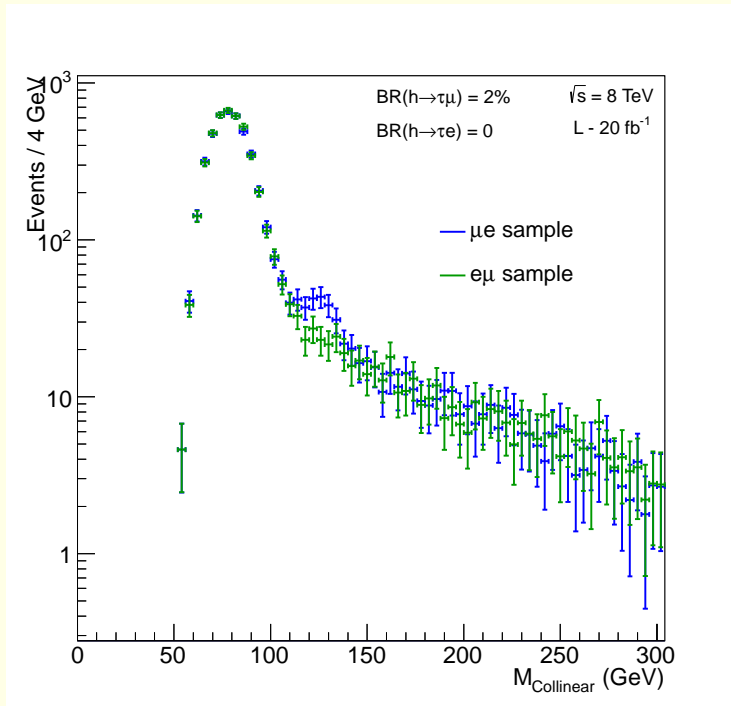
- The SM gauge interactions are lepton flavor universal
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- Yukawa interactions are not universal
- $\text{BR}(h \rightarrow \tau\mu) \neq \text{BR}(h \rightarrow \tau e)$ – possible
- In fact, the bounds from $\mu \rightarrow e\gamma$ imply that $\text{BR}_{\tau\mu}$ and $\text{BR}_{\tau e}$ cannot be simultaneously close to the respective upper bounds
- $\implies \text{BR}(h \rightarrow \tau\mu) \neq \text{BR}(h \rightarrow \tau e)$ breaks the $e \leftrightarrow \mu$ symmetry

The method

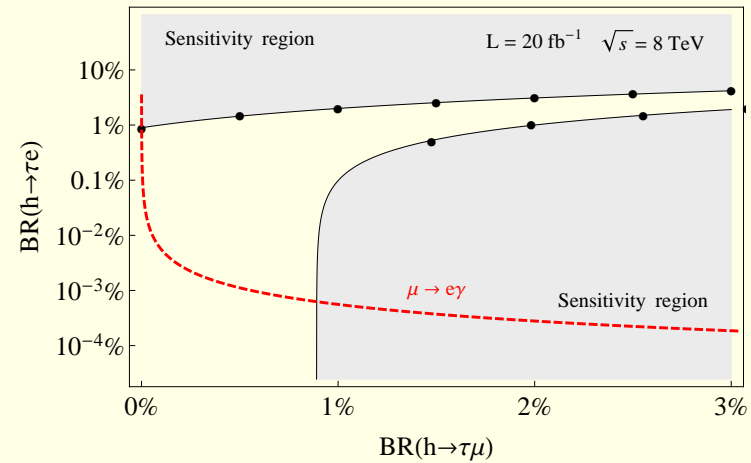
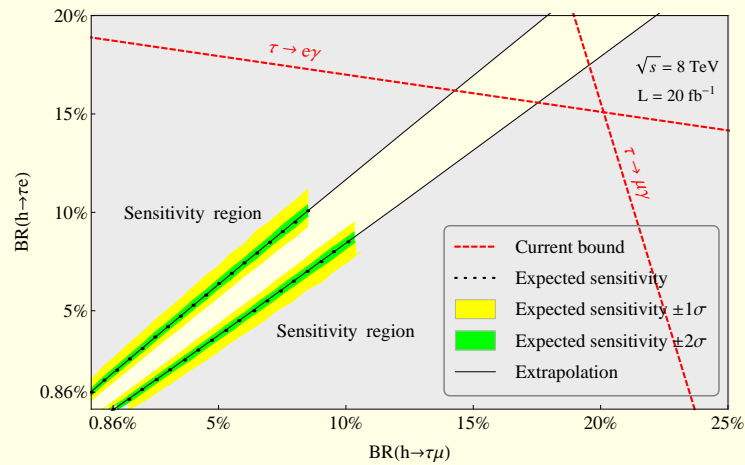
- Divide the data to two mutually exclusive samples:
 - (μe) data sample: $p_T^\mu > p_T^e$
 - $(e\mu)$ data sample: $p_T^e > p_T^\mu$
- SM background: divided equally between the two samples
- $h \rightarrow \tau^\pm \mu^\mp$ events are mostly in the (μe) sample;
 $h \rightarrow \tau^\pm e^\mp$ events are mostly in the $(e\mu)$ sample
- Subtracting $(\mu e) - (e\mu)$ provides a measurement of $\text{BR}_{\tau\mu} - \text{BR}_{\tau e}$
- For $\text{BR}_{\tau e} = 0$, the $(e\mu)$ sample provides the SM background

Data driven background estimate



(μe) and $(e\mu)$ distributions

The sensitivity



1405.4545

- With one rate negligibly small, and with 20 fb^{-1} of collected data: 3σ sensitivity for discovering $\text{BR}_{\tau\mu}$ (or $\text{BR}_{\tau e}$) $\simeq 0.9\%$.

What if $\text{BR}(h \rightarrow \tau\mu) \sim 0.01$?

What if $\text{BR}_{\tau\mu} \sim 0.01$?

Exciting $\times 3$

- $U(1)_\mu \times U(1)_\tau$ broken
 $\Lambda_{\text{LFV}} \ll \Lambda_{\text{LNV}}$?
- $\text{BR}(h \rightarrow \tau\mu) \ll \text{BR}(h \rightarrow \tau\tau)$
FCNC at tree level?
- $Y_E \not\propto M_E$
Not the SM Higgs?

What if $\text{BR}_{\tau\mu} \sim 0.01$?

The scale of LFV

- $\frac{1}{\Lambda_{\text{LNV}}} LL\phi\phi$

$$m_\nu \sim 0.1 \text{ eV} \implies \Lambda_{\text{LNV}} \sim 10^{15} \text{ GeV}$$

Intriguingly close to Λ_{GUT}

- $\frac{1}{\Lambda_{\text{LFV}}^2} \phi^\dagger \phi L\phi E^c$

$$\text{BR}(h \rightarrow \tau\mu) \sim 0.01 \implies \Lambda_{\text{LFV}} \sim 5 \text{ TeV}$$

New physics should be directly accessible at the LHC!

What if $\text{BR}_{\tau\mu} \sim 0.01$?

Reminder: SM-FCNC are loop suppressed

- The **gluon** and the **photon** do not mediate FCNC at tree level because massless gauge bosons have flavor-universal and, in particular, flavor diagonal couplings
- Within the SM, the **Z-boson** does not mediate FCNC at tree level because all fermions with the same chirality, color and charge originate in the same $SU(2)_L \times U(1)_Y$ representation
- Within the SM, the **h-boson** does not mediate FCNC at tree level because
 - All SM fermions are chiral \implies no bare mass terms
 - The scalar sector has a single Higgs doublet

What if $\text{BR}_{\tau\mu} \sim 0.01$?

Loop suppression?

- All models with no bare mass terms and with NFC:

$h \rightarrow \tau\mu$ is loop suppressed

- With loop suppression:

$$(v^2/\Lambda^2)(\alpha_W/4\pi)X_{\mu\tau} \not\ll y_\tau \sim 10^{-2}$$

Very challenging model building

- MSSM - strongly disfavored Aloni, YN, Stamou, work in progress

Brignole, Rossi, NPB701(2004)3; Arana-Catania, Arganda, Herrero, JHEP 09(2013)160

- Models with tree-level-FCNC favored

What if $\text{BR}_{\tau\mu} \sim 0.01$?

Not the SM Higgs?

$Y_{\mu\tau}^h \neq 0$ at tree level:

- Single Higgs doublet and vector-like leptons
Strongly disfavored by the $\tau \rightarrow \mu\mu\mu$ bound

Efrati, YN, Stamou, work in progress

Dorsner et al., 1502.07784

- Multi-Higgs doublet models
Not easy to combine with flavor models

What if $\text{BR}_{\tau\mu} \sim 0.01$?

Vector-like leptons

- In all models of vector-like leptons, there are unavoidable tree level contributions to $Z \rightarrow \tau\mu$ and $\tau \rightarrow \mu\mu\mu$
- For each type of vector-like leptons, there is a parameter-independent relation:

$$\frac{\text{BR}(h \rightarrow \tau\mu) / \text{BR}(h \rightarrow \tau\tau)}{\text{BR}(Z \rightarrow \tau\mu) / \frac{1}{3} \text{BR}(Z \rightarrow \nu\bar{\nu})} = \frac{1}{2}$$

Efrati, YN, Stamou, work in progress

- Experiment: $\frac{\text{BR}(Z \rightarrow \tau\mu)}{\frac{1}{3} \text{BR}(Z \rightarrow \nu\bar{\nu})} < 1.8 \times 10^{-4}$
 $\implies \text{BR}(h \rightarrow \tau\mu) < 2 \times 10^{-5}$
- Still, possible to account for $\text{BR}(h \rightarrow \tau\mu) \sim 0.01$ with fine-tuned cancelations

What if $\text{BR}_{\tau\mu} \sim 0.01$?

2HDM

- Are there viable and natural flavor models that have
 - $Y_{\mu\tau} \sim 0.01$ but $Y_{e\mu} \lesssim 10^{-6}$?
- Natural Flavor Conservation (NFC)
 - Impossible ($Y_{\mu\tau} = 0$)
- Minimal Lepton Flavor Violation (MLFV)
 - Y^E -spurion: Impossible ($Y_{\mu\tau} = 0$)
 - Y^E, Y^N, M^N -spurions: Possible with fine-tuning
- Froggatt-Nielsen (FN):
 - $Y_{e\mu}/Y_{\mu\tau} \sim |U_{e2}/U_{\mu3}|(m_\mu/m_\tau) \sim 0.05 \implies$ too large
 - Possible with supersymmetry and holomorphic zeros

Dery, Efrati, YN, Soreq, Susič, PRD90, 115022 [arXiv:1408.1371]

Conclusions

Conclusions

$$\underline{h \rightarrow \mu\tau}$$

If $\text{BR}(h \rightarrow \tau\mu) \sim 0.01$:

- SM, NFC, MLFV* - excluded
- New physics at the TeV scale
- Most likely, FCNC at tree level
- Most likely, extra scalar doublets
- Challenge to present explanations of the flavor puzzles

h Physics = New Flavor Arena

Measure:

- Third generation couplings: Y_t, Y_b, Y_τ
- Second generation couplings: Y_c, Y_s, Y_μ
- Flavor violating couplings: $Y_{\mu\tau}, Y_{e\tau}, Y_{ct}, Y_{ut}$

Test:

- MFV
- FN
- NFC
- ...

Recent related work

- Blankenburg, Ellis, Isidori, Phys. Lett. B712, 386 (2012)
- Bhattacharyya, Leser, Pas, Phys. Rev D86, 036009 (2012)
- Harnik, Kopp, Zupan, JHEP 1303, 026 (2013)
- Davidson, Verdier, Phys. Rev. D80, 111701 (2012)
- Celis, Cirigliano, Passemar, Phys. Rev. D89, 013008 (2014)
- Falkowski, Straub, Vicente, JHEP 1405, 092 (2014)
- Delaunay *et al.*, Phys. Rev. D89, 033014 (2014)
- Gorbahn, Haisch, JHEP 1406, 033 (2014)
- Kagan *et al.*, arXiv:1406.1722
- Crivellin, D'Ambrosio, Heeck, arXiv: 1501.00993

$h \rightarrow \mu\tau$ in EFT

- SM: Forbidden by the accidental $U(1)_\mu \times U(1)_\tau$
- $d = 5$ terms $\frac{(Y^N)_{ij}}{\Lambda} L_i L_j \phi \phi$: Allowed, but \implies
 - Loop suppression $\sim \alpha_2^2$
 - Mixing suppression $\sim |U_{\mu 3} U_{\tau 3}|^2$
 - GIM suppression $\sim (\Delta m_{23}^2 / m_W^2)^2$
- $d = 6$ terms $\frac{1}{\Lambda^2} (\phi^\dagger \phi) \phi \bar{\mu}_L Z_{\mu\tau}^e \tau_R$:
 The leading contribution –

$$M_E = \frac{v}{\sqrt{2}} \left(Y^e + \frac{v^2}{2\Lambda^2} Z^e \right), \quad Y_h^E = Y^e + 3 \frac{v^2}{2\Lambda^2} Z^e$$

$$\implies Y_h^E = (\sqrt{2} M_E / v) + \frac{v^2}{2\Lambda^2} Z^e$$
- Note: $\frac{1}{\Lambda^2} \phi \bar{\mu}_L X_{\mu\tau}^e \sigma_{\mu\nu} \tau_R F^{\mu\nu} \implies \tau \rightarrow \mu\gamma$